Solutions

1. An AVL tree contains 30 nodes. What is the maximum height that it could be?

You need to compute the $\mathrm{S}(\mathrm{h})$ function until you find an $h$ for which $S(h) \leq 30<S(h+1)$. Then it is this value of $h$. A simple table works best, as I showed in class:

| h | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~S}(\mathrm{~h})$ | 1 | 2 | 4 | 7 | 12 | 20 | 33 |

This shows that a tree of height 6 must have at least 33 nodes, so a tree with 30 nodes is at most height 5 .
2. The values $60,45,85,65,55,30,35,70$ are inserted into an initially empty, unbalanced binary search tree. Draw the final tree in the space below. This is straightforward:

3. The initial tree:


The tree after the deletion of node 30 is below. There were two rotations, one at 40 after deleting 30 , then one at the root.


